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Dynamic Buffer Capacities in Redox Systems

Anna Maria Michałowska-Kaczmarczyk¹,
Aneta Spórna-Kucab² and
Tadeusz Michałowski^{2*}

Abstract

The buffer capacity concept is extended on dynamic redox systems, realized according to titrimetric mode, where changes in pH are accompanied by changes in potential E values; it is the basic novelty of this paper. Two examples of monotonic course of the related curves of potential E vs. and pH vs. Φ relationships were considered. The systems were modeled according to GATES/GEB principles.

Keywords: Thermodynamics of electrolytic redox systems; Buffer capacity; GATES/GEB.

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Introduction

The buffer capacity concept is usually referred to as a measure of resistance of a solution (D) on pH change, affected by an acid or base, added as a titrant T, i.e., according to titrimetric mode; in this case, D is termed as titrand.

The titration is a dynamic procedure, where V mL of titrant T, containing a reagent B (C mol/L), is added into V₀ mL of titrand D, containing a substance A (C₀ mol/L). The advance of a titration B(C,V) \Rightarrow A(C₀,V₀), denoted for brevity as B \Rightarrow A is characterized by the fraction titrated [1-4]

$$\Phi = \frac{C \cdot V}{C_0 \cdot V_0} \quad (1)$$

That introduces a kind of normalization (independence on V₀ value) for titration curves, expressed by pH=pH(Φ), and E=E(Φ) for potential E [V] expressed in SHE scale. The redox systems with one, two or more electron-active elements are modeled according to principles of Generalized Approach to Electrolytic Systems with Generalized Electron Balance involved (GATES/GEB), described in details in [5-16], and in references to other authors' papers cited therein.

According to earlier conviction expressed by Gran [17], all titration curves: pH=pH(Φ) and E=E(Φ), were perceived as monotonic; that generalizing statement is not true [7], however. According to contemporary knowledge, full diversity in this regard is stated, namely: (1o) monotonic pH=pH(Φ) and monotonic E=E(Φ) [18-20]; (2o) monotonic pH=pH(Φ) and non-monotonic E=E(Φ) [6]; (3o) non-monotonic pH=pH(Φ) and monotonic E=E(Φ) [5]; (4o) non-monotonic pH=pH(Φ), and non-monotonic E=E(Φ) [7].

- 1 Department of Oncology, The University Hospital in Cracow, Cracow, Poland
- 2 Department of Analytical Chemistry, Technical University of Cracow, Cracow, Poland

Corresponding author:

Tadeusz Michałowski

✉ michalot@o2.pl

Department of Analytical Chemistry, Technical University of Cracow, 24, 31-155 Cracow, Poland.

Tel: +48 12 628 20 00

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Examples of Titration Curves pH=pH(Φ) and E=E(Φ) in redox systems

In this paper, we refer to the disproportionating systems: (S1) NaOH \Rightarrow HIO and (S2) HCl \Rightarrow NaIO, characterized by monotonic changes of pH and E values during the related titrations (i.e., the case 1o). In both instances, the values: V₀=100, C₀=0.01, and C=0.1 were assumed. The set of equilibrium data [18-20] applied in calculations, presented in **Table 1**, is completed by the solubility of solid iodine, I₂(s), in water, equal 1.33·10⁻³ mol/L. The related algorithms, prepared in MATLAB for S1 (NaOH \Rightarrow HIO) S2 (HCl \Rightarrow NaIO) system according to the GATES/GEB principles, are presented in Appendices 1 and 2.

The titration curves: pH=pH(Φ) and E=E(Φ) presented in **Figures 1 and 2** are the basis to formulation of dynamic buffer capacities in the systems S1 and S2.

Dynamic acid-base buffer capacities β_v and B_v

Dynamic buffer capacity was referred previously only to acid-

Table 1 Physicochemical data related to the systems S1 and S2.

No.	Reaction	Equilibrium equation	Equilibrium data
1	$I_2 + 2e^{-1} = 2I^{-1}$ (for dissolved I_2)	$[I^{-1}]^2 = K_{e1} \cdot [I_2][e^{-1}]^2$	$E_{01} = 0.621$ V
2	$I_3^{-1} + 2e^{-1} = 3I^{-1}$	$[I^{-1}]^3 = K_{e2} \cdot [I_3^{-1}][e^{-1}]^2$	$E_{02} = 0.545$ V
3	$IO^{-1} + H_2O + 2e^{-1} = I^{-1} + 2OH^{-1}$	$[I^{-1}][OH^{-1}]^2 = K_{e3} \cdot [IO^{-1}][e^{-1}]^2$	$E_{03} = 0.49$ V
4	$IO_3^{-1} + 6H^{+1} + 6e^{-1} = I^{-1} + 3H_2O$	$[I^{-1}] = K_{e4} \cdot [IO_3^{-1}][H^{+1}]^6[e^{-1}]^6$	$E_{04} = 1.08$ V
5	$H_5IO_6 + 7H^{+1} + 8e^{-1} = I^{-1} + 6H_2O$	$[I^{-1}] = K_{e5} \cdot [H_5IO_6][H^{+1}]^7[e^{-1}]^8$	$E_{05} = 1.24$ V
6	$H_3IO_6^{-2} + 3H_2O + 8e^{-1} = I^{-1} + 9OH^{-1}$	$[I^{-1}][OH^{-1}]^9 = K_{e6} \cdot [H_3IO_6^{-2}][e^{-1}]^8$	$E_{06} = 0.37$ V
7	$HIO = H^{+1} + IO^{-1}$	$[H^{+1}][IO^{-1}] = K_{111} \cdot [HIO]$	$pK_{111} = 10.6$
8	$HIO_3 = H^{+1} + IO_3^{-1}$	$[H^{+1}][IO_3^{-1}] = K_{511} \cdot [HIO_3]$	$pK_{511} = 0.79$
9	$H_4IO_6^{-1} = H^{+1} + H_3IO_6^{-2}$	$[H^{+1}][H_3IO_6^{-2}] = K_{72} \cdot [H_4IO_6^{-1}]$	$pK_{72} = 3.3$
10	$Cl_2 + 2e^{-1} = 2Cl^{-1}$	$[Cl^{-1}]^2 = K_{e7} \cdot [Cl_2][e^{-1}]^2$	$E_{07} = 1.359$ V
11	$ClO^{-1} + H_2O + 2e^{-1} = Cl^{-1} + 2OH^{-1}$	$[Cl^{-1}][OH^{-1}]^2 = K_{e8} \cdot [ClO^{-1}][e^{-1}]^2$	$E_{08} = 0.88$ V
12	$ClO_2^{-1} + 2H_2O + 4e^{-1} = Cl^{-1} + 4OH^{-1}$	$[Cl^{-1}][OH^{-1}]^4 = K_{e9} \cdot [ClO_2^{-1}][e^{-1}]^4$	$E_{09} = 0.77$ V
13	$HClO = H^{+1} + ClO^{-1}$	$[H^{+1}][ClO^{-1}] = K_{11Cl} \cdot [HClO]$	$pK_{11Cl} = 7.3$
14	$HClO_2 + 3H^{+1} + 4e^{-1} = Cl^{-1} + 2H_2O$	$[Cl^{-1}] = K_{e10} \cdot [HClO_2][H^{+1}]^3[e^{-1}]^4$	$E_{010} = 1.56$ V
15	$ClO_2 + 4H^{+1} + 5e^{-1} = Cl^{-1} + 4H_2O$	$[Cl^{-1}] = K_{e11} \cdot [ClO_2][H^{+1}]^4[e^{-1}]^4$	$E_{011} = 1.50$ V
16	$ClO_3^{-1} + 6H^{+1} + 6e^{-1} = Cl^{-1} + 3H_2O$	$[Cl^{-1}] = K_{e12} \cdot [ClO_3^{-1}][H^{+1}]^6[e^{-1}]^6$	$E_{012} = 1.45$ V
17	$ClO_4^{-1} + 8H^{+1} + 8e^{-1} = Cl^{-1} + 4H_2O$	$[Cl^{-1}] = K_{e13} \cdot [ClO_4^{-1}][H^{+1}]^8[e^{-1}]^8$	$E_{013} = 1.38$ V
18	$2ICl + 2e^{-1} = I_2 + 2Cl^{-1}$	$[I_2][Cl^{-1}]^2 = K_{e14} \cdot [ICl]^2[e^{-1}]^2$	$E_{014} = 1.105$ V
19	$I_2Cl^{-1} = I_2 + Cl^{-1}$	$[I_2][Cl^{-1}] = K_1 \cdot [I_2Cl^{-1}]$	$\log K_1 = 0.2$
20	$ICl_2^{-1} = ICl + Cl^{-1}$	$[ICl][Cl^{-1}] = K_2 \cdot [ICl_2^{-1}]$	$\log K_2 = 2.2$
21	$H_2O = H^{+1} + OH^{-1}$	$[H^{+1}][OH^{-1}] = K_w$	$pK_w = 14.0$

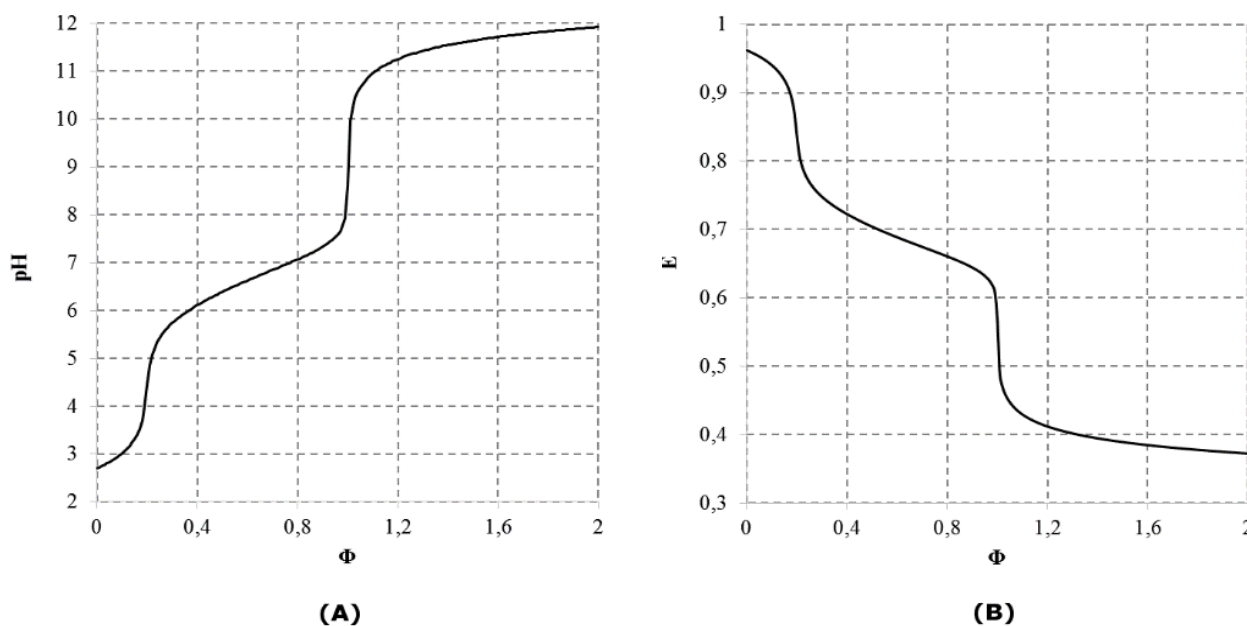


Figure 1 (A) $pH = pH(\Phi)$ and (B) $E = E(\Phi)$ relationships plotted for the system $NaOH \Rightarrow HIO$.

base equilibria in non-redox systems [3,21-23]. However, the dynamic (β_v) and windowed (B_v) buffer capacities can be also related to acid-base equilibria in redox systems. The β_v is formulated as follows [3,21].

$$\beta_v = \left| \frac{dc}{dpH} \right| \quad (2)$$

where

$$c = \frac{CV}{V_0 + V} \quad (3)$$

It is the current concentration of B in D+T mixture, at any point of the titration. In the simplest case, D is a solution of one substance A (C_0 mol/L), and then Equation 3 can be rewritten as follows

$$c = \Phi \cdot \frac{C_0 C}{C + \Phi \cdot C_0} \quad (4)$$

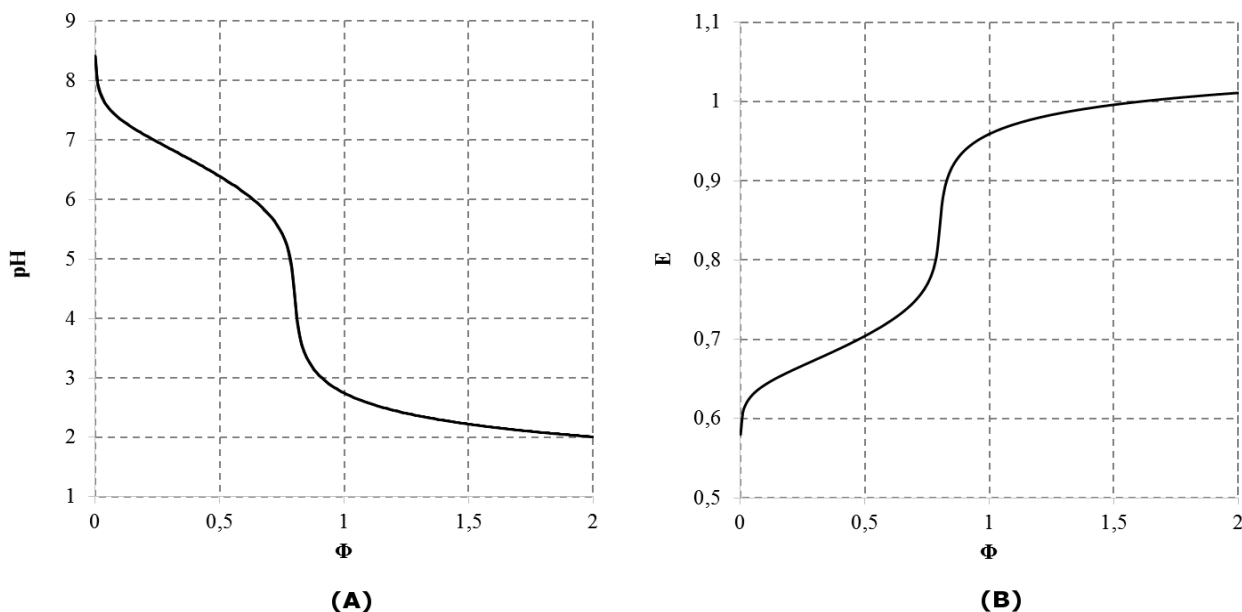


Figure 2 (A) $pH=pH(\Phi)$ and (B) $E=E(\Phi)$ relationships plotted for the system $HCl \Rightarrow NaIO$.

where Φ is the fraction titrated (Equation 1). Then we get

$$\beta_v = \frac{dc}{d\Phi} \cdot \left| \frac{d\Phi}{dpH} \right| = \frac{C_0 \cdot C^2}{(C + \Phi \cdot C_0)^2} \cdot \frac{1}{|\eta|} = \frac{c^2}{C_0 \cdot |\eta|} \quad (5)$$

where

$$\eta = \frac{dpH}{d\Phi} \quad (6)$$

is the sharpness index on the titration curve. For comparative purposes, the absolute values $|\beta_v|$ and $|\eta|$, for β_v (Equations 1 and 5) and η (Equation 6) are considered. At $C_0/C \ll 1$ and small Φ value, from Equation 3 we get $\hat{a}_v = \hat{O}^2 \cdot C_0 / |\zeta|$.

The β_v value is the point-assessment and then cannot be used in the case of finite pH-changes (ΔpH) corresponding to an addition of a finite volume of titrant (β_v is a non-linear function of pH). For this purpose, the 'windowed' buffer capacity, B_v , defined by the formula [3,21].

$$B_v = \left| \frac{\Delta c}{\Delta pH} \right| \quad (7)$$

where

$$\frac{\Delta c}{\Delta pH} = \frac{1}{\Delta pH} \cdot \int_{pH}^{pH+\Delta pH} \beta_v \cdot dpH = \frac{c(pH + \Delta pH) - c(pH)}{\Delta pH} \quad (8)$$

has been suggested. From extension in Taylor series we have

$$\frac{\Delta c}{\Delta pH} = \beta_v + \frac{d\beta_v}{dpH} \cdot \frac{\Delta pH}{2} + \frac{d^2\beta_v}{dpH^2} \cdot \frac{(\Delta pH)^2}{6} + \dots = \beta_v + \sum_{k=1}^{\infty} \left(\frac{d^k \beta_v}{dpH^k} \right)_{pH} \cdot \frac{(\Delta pH)^k}{(k+1)!} \quad (9)$$

where

$$\left(\frac{d^k c}{dpH^k} \right)_{pH} = \left(\frac{d^{k-1} \beta_v}{dpH^{k-1}} \right)_{pH} \quad (10)$$

From Equations 7 and 9 we see that β_v is the first approxima-

tion of B_v . One should take here into account that finite changes (ΔpH) in pH, e.g. $\Delta pH=1$, are involved with addition of a finite volume of a reagent endowed with acid-base properties, here: base NaOH, of a finite concentration, C .

Dynamic redox buffer capacities β_v^E and B_v^E

In similar manner, one can formulate dynamic buffer capacities B_v^E and β_v^E , involved with infinitesimal and finite changes of potential E values:

$$\beta_v^E = \left| \frac{dc}{dE} \right| \quad (11)$$

$$B_v^E = \left| \frac{\Delta c}{\Delta E} \right| \quad (12)$$

Where c is defined by Equation 2, and then we have

$$\frac{\Delta c}{\Delta E} = \frac{1}{\Delta E} \cdot \int_E^{E+\Delta E} \beta_v^E \cdot dE = \frac{c(E + \Delta E) - c(E)}{\Delta E} \quad (13)$$

$$\frac{\Delta c}{\Delta E} = \beta_v^E + \sum_{k=1}^{\infty} \left(\frac{d^k \beta_v^E}{dE^k} \right)_E \cdot \frac{(\Delta E)^k}{(k+1)!}$$

where

$$\frac{d^k c}{dE^k} = \left(\frac{d^{k-1} \beta_v^E}{dE^{k-1}} \right)_E \quad (14)$$

Graphical presentation of dynamic buffer capacities in redox systems

Referring to dynamic redox systems represented by titration curves presented in **Figures 1 and 2**, we plot the relationships: β_v vs. Φ , β_v vs. pH, β_v vs. E , and β_v^E vs. Φ , β_v^E vs. pH, β_v^E vs. E for the systems: (S1) $NaOH \Rightarrow HIO$; (S2) $HCl \Rightarrow NaIO$. The relations: (A) β_v vs. Φ , (B) β_v vs. pH, (C) β_v vs. E and (D) β_v^E vs. Φ , (E) β_v^E vs. pH, (F) β_v^E vs. E are plotted in **Figures 3 and 4**.

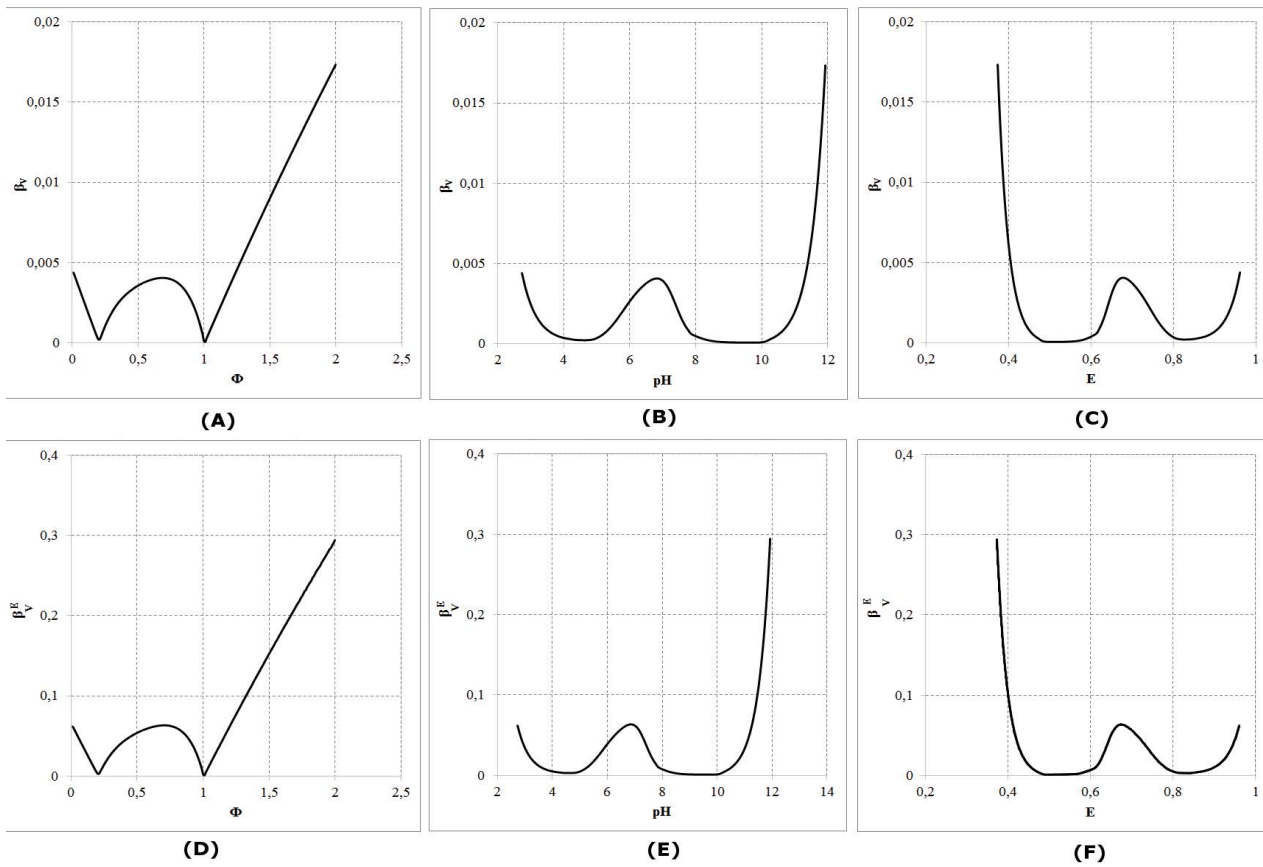


Figure 3 The relations: (A) β_V vs. Φ , (B) β_V vs. pH, (C) β_V vs. E and (D) β_V^E vs. Φ , (E) β_V^E vs. pH, (F) β_V^E vs. E for (S1) $\text{NaOH} \Rightarrow \text{HIO}$.

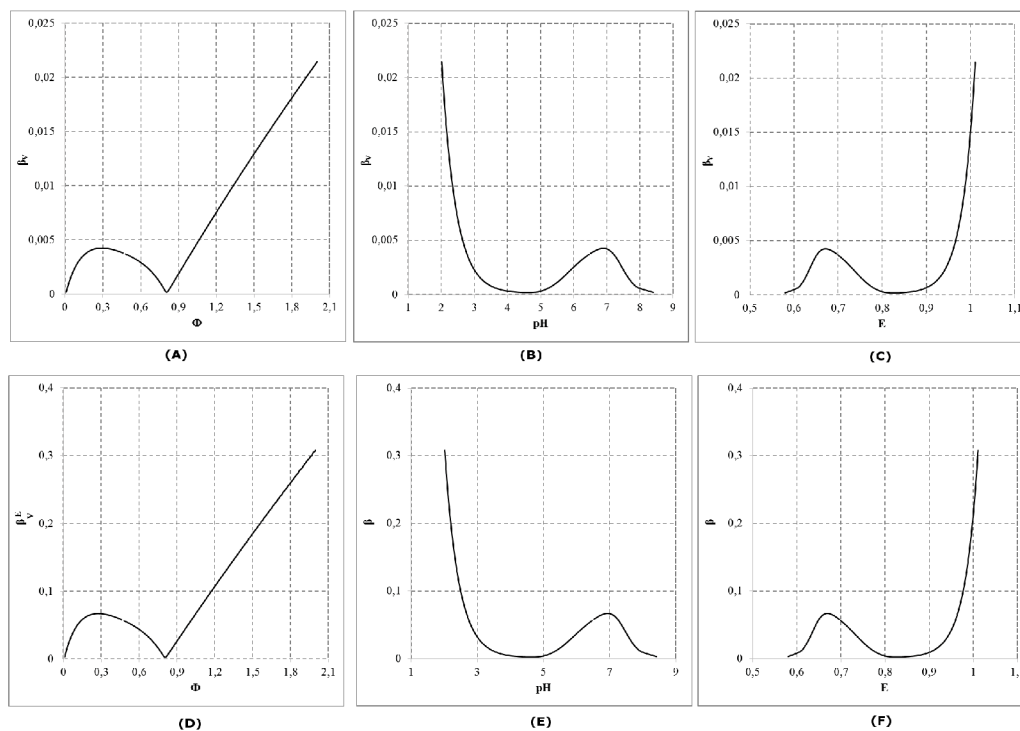


Figure 4 The relations: (A) β_V vs. Φ , (B) β_V vs. pH, (C) β_V vs. E and (D) β_V^E vs. Φ , (E) β_V^E vs. pH, (F) β_V^E vs. E for (S2) $\text{HCl} \Rightarrow \text{NaIO}$.

Discussion

Disproportionation of the solutes considered (HIO or NaIO) in D occurs directly after introducing them into pure water. The disproportionation is intensified, by greater pH changes, after addition of the respective titrants: NaOH (in S1) or HCl (in S2), and the monotonic changes of $E=E(\Phi)$ and $pH=pH(\Phi)$ occur in all instances.

All attainable equilibrium data related to these systems are included in the algorithms implemented in the MATLAB computer program (see Appendices 1 and 2). In all instances, the system of equations was composed of: generalized electron balance (GEB), charge balance (ChB) and concentration balances for particular elements \neq H, O.

In the system S1, the precipitate of solid iodine, $I_{2(s)}$, is formed, see **Figure 5**. In the (relatively simple) redox system S2, we have all four basic kinds of reactions; except redox and acid-base reactions, the solid iodine ($I_{2(s)}$) is precipitated and soluble complexes: I_2Cl^{-1} , ICl and ICl_2^{-1} are formed, see **Figure 6A**. Note that $I_{2(s)} + I^{-1} = I_3^{-1}$ is also the complexation reaction.

In the system S2, all oxidized forms of Cl^{-1} were involved, i.e. the oxidation of Cl^{-1} ions was thus pre-assumed. This way, full "democracy" was assumed, with no simplifications [18-20]. However, from the calculations we see that HCl acts primarily as a disproportionating, and not as reducing agent. The oxidation of Cl^{-1} occurred here only in an insignificant degree (**Figure 6B**); the main product of the oxidation was Cl_2 , whose concentration was on the level ca. 10^{-16} - 10^{-17} mol/L.

Conclusion

The redox buffer capacity concepts: \hat{a}_V and \hat{a}_{Φ} can be principally related to monotonic functions. This concept looks awkwardly for non-monotonic functions $pH=pH(\Phi)$ and/or $E=E(\Phi)$ specified above (2^o-4^o) and exemplified in **Figures 7-9** presented in appendix 3. For comparison, in isohydric (acid-base) systems, the

buffer capacity strives for infinity. In particular, it occurs in the titration $HB(C,V) \Rightarrow HL(C_0,V_0)$, where HB is a strong monoprotic acid and HL is a weak monoprotic acid characterized by the dissociation constant $K_1=[H^+][L^{-1}]/[HL]$; at $4K_w/C^2 \ll 1$, the isohydricity condition is expressed here by the Michałowski formula $C_0 = C + C^2 \cdot 10^{-K_1}$ [24-26].

The formula for the buffer capacity, suggested by Bard et al. [27] after Levie [28], is not correct. Moreover, it involves formal potential value, perceived as a kind of conditional equilibrium constant idea, put in (apparent) analogy with the simplest static acid-base buffer capacity, see criticizing remarks in the study by Michałowska-Kaczmarczyk et al. [29]; it is not adaptable for real redox systems.

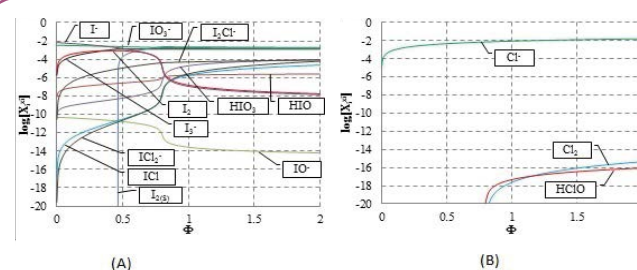


Figure 6 Speciation diagram for the system (S2) $HCl \Rightarrow NaIO$: (A) for iodine species; (B) for oxidized forms of chlorine species.

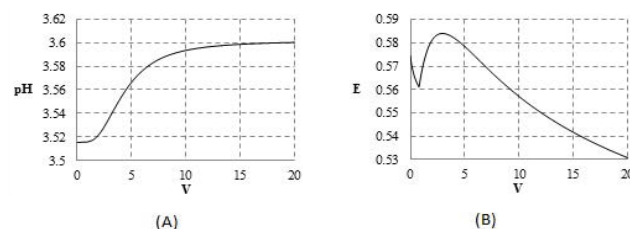


Figure 7 Case (2^o): (A) monotonic $pH=pH(V)$ and (B) non-monotonic $E=E(V)$ plots on the step 3 of the process presented in the study by Michałowska-Kaczmarczyk et al. [6].

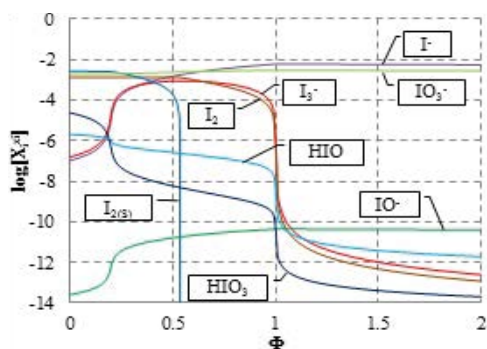


Figure 5 Speciation diagram for the system (S1) $NaOH \Rightarrow HIO$.

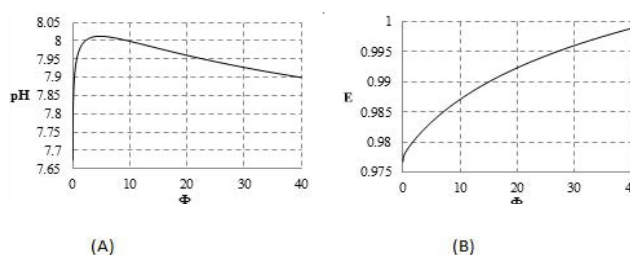


Figure 8 Case (3^o): (A) non-monotonic $pH=pH(\Phi)$ and (B) monotonic $E=E(\Phi)$ functions for the system $KBrO_3 \Rightarrow NaBr$ presented in study by Michałowska-Kaczmarczyk et al. [5].

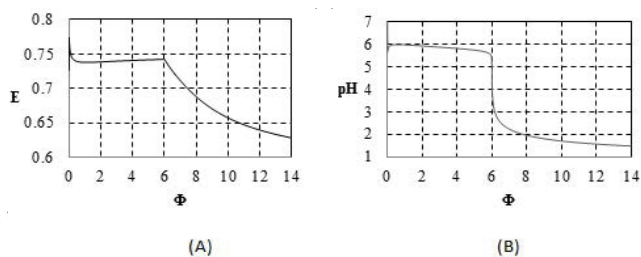


Figure 9 Case (4°): the (A) non-monotonic $pH=pH(\Phi)$ and (B) non-monotonic $E=E(\Phi)$ functions for the system $HI \rightleftharpoons KIO_3$ presented in the study by Michałowski [7].

Buffered solutions are commonly applied in different procedures involved with classical (titrimetric, gravimetric) and instrumental analyses [30-33]. There are in close relevance to isohydric solutions [24-26] and pH-static titration [4,34], and titration in binary-solvent systems [12,35]. Buffering property is usually referred to an action of an external agent (mainly: strong acid, HB, or strong base, MOH) inducing pH change, ΔpH , of the solution. Redox buffer capacity is also involved with the problem of interfacing in CE-MS analysis, and bubbles formation in reaction 2 $H_2O=O_{2(g)} + 4H^{+1} + 4e^{-1}$ at the outlet electrode in CE [36-39].

In the paper, a nice proposal of “slyke”, as the name for (acid-base, pH) buffer capacity unit, has been raised [40].

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